

# CSC 437/537 - Geometric Algorithms

Instructor: Joshua A. Levine

Office: 754 Gould-Simpson

Meets: M/W 2:00-3:15pm, 222 Social Sciences

Office Hours: M 3:30-4:30pm, T 4:30-5:30pm (GS 754), or by appointment

TA: Alex Koltz, akoltz@email.arizona.edu

TA Office Hours: M 1:00-2:00pm (GS 938)

TA: Justin Crum, jcrum@math.arizona.edu

TA Office Hours: F 10:00am-11:00am (GS 938)

[Course Syllabus](#)

[D2L \(for 437\)](#)

[D2L \(for 537\)](#)

[Piazza](#)

## Course Calendar

All topics on this page are tentative and subject to change!

All required readings are intended to be read **before** class begins

Week	Date	Monday	Date	Wednesday
1	Jan 07	-- No Class --	Jan 09	<a href="#">Introduction</a>
2	Jan 14	<a href="#">2D Convex Hulls</a>	Jan 16	<a href="#">Line Segment Intersection</a>
3	Jan 21	-- MLK Day --	Jan 23	<a href="#">Overlay of Subdivisions</a>
4	Jan 28	<a href="#">Polygon Triangulation</a>	Jan 30	<a href="#">low-D Incremental LP</a>
5	Feb 04	<a href="#">low-D Randomized LP</a>	Feb 06	<a href="#">Range Trees</a>
6	Feb 11	<a href="#">Trapezoidal Maps</a>	Feb 13	<a href="#">Point Location</a>
7	Feb 18	<a href="#">Voronoi Diagrams</a>	Feb 20	<a href="#">Variations on Voronoi</a>
8	Feb	<a href="#">Point-Line Duality</a>	Feb	<a href="#">Midterm Exam</a>

[Final project info for 537 students](#)

Proposals Due: Feb 22

[Homework 1 - Chs. 1-2](#)

Assigned: Jan 23

Due: Feb 06 01:59:59

PM

Graded: Feb 13

[Homework 2 - Chs. 3-5](#)

Assigned: Feb 06

Due: Feb 20 01:59:59

PM

Graded: Feb 27

[Homework 3 - Chs. 6-7](#)

Assigned: Feb 20

Due: Mar 13 01:59:59

PM

Graded: Mar 30

[Homework 4 - Chs. 8-9](#)

Assigned: Mar 13

Due: Mar 27 01:59:59

PM

Graded: Apr 03

[Homework 5 - Chs. 10-12](#)

Assigned: Mar 27

Due: Apr 10 01:59:59

PM

Graded: Apr 17

[Homework 6 - Chs. 13-15](#)

Assigned: Apr 10

Due: Apr 24 01:59:59

	25		27
9	Mar -- Spring Break --		Mar -- Spring Break --
	04		06
10	Mar Delaunay		Mar More Delaunay
	11 Triangulations		13
11	Mar Alpha Hulls		Mar Segment Trees
	18		20
12	<span style="border: 1px solid black; padding: 2px;">Mar 25</span> 3D Convex Hulls		Mar Binary Space Partitions
			27
13	Apr 01 Motion Planning		Apr 03 Quadtrees
14	Apr 08 Visibility Graphs		Apr 10 Grad Presentations
15	Apr 15 Grad Presentations		Apr 17 Grad Presentations
16	Apr 22 Grad Presentations		Apr 24 Grad Presentations
17	Apr 29 Grad Presentations		May Final Exam Review
			01

PM

Graded: May 01

### Final Exam: Fri., May 3, 1-3pm, 222 Social Sciences

Highlighted dates have a homework assignment **due** immediately before class begins on that day.

Boxed dates correspond to *the day before* the deadlines for the dropping (without a W) and the withdraw deadlines for this semester.

See [Spring 2019 Undergraduate Dates and Deadlines](#) and [Spring 2019 Graduate Dates and Deadlines](#).

[Link to Google drive folder with all lecture slides](#)

#### Lecture 01 - Introduction (slides)

Date: January 09, 2019

Required Reading:

- [Course Syllabus](#)

#### Lecture 02 - 2D Convex Hulls (slides)

Date: January 14, 2019

Required Reading:

- [BCKO, Sections 1.0-1.4](#)

Optional Reading:

- [Mount, Lectures 1,3 \(pg. 2-6,11-16\)](#)

- Jarvis, R. A. (1973). [On the identification of the convex hull of a finite set of points in the plane](#). Information processing letters, 2, 18-21.
- Graham, R. L. (1972). [An efficient algorithm for determining the convex hull of a finite planar set](#). Info. Pro. Lett., 1, 132-133.
- Chan, T. M. (1996). [Optimal output-sensitive convex hull algorithms in two and three dimensions](#). Discrete & Computational Geometry, 16(4), 361-368.
- Many variants referenced in [BCKO, Section 1.5](#)

### Lecture 03 - Line Segment Intersection ([slides](#))

Date: January 16, 2019

Required Reading:

- [BCKO, Sections 2.1](#)

Optional Reading:

- [Mount, Lecture 5 \(pg. 25-32\)](#)
- Bentley, J. L. & Ottmann, T. A. (1979). [Algorithms for reporting and counting geometric intersections](#). IEEE Transactions on computers, (9), 643-647.
- Chazelle, B. & Edelsbrunner, H. (1992). [An optimal algorithm for intersecting line segments in the plane](#). Journal of the ACM (JACM), 39(1), 1-54.

### Lecture 04 - Overlay of Subdivisions ([slides](#))

Date: January 23, 2019

Required Reading:

- [BCKO, 2.2-2.3](#)

Optional Reading:

- [Mount, Lecture 23 \(pg. 134-137\)](#)
- Paper that first suggested the DCEL: Muller, D. E., & Preparata, F. P. (1978). [Finding the intersection of two convex polyhedra](#). Theoretical Computer Science, 7(2), 217-236.
- Winged-edge data structure: Baumgart, B. G. (1975, May). [A polyhedron representation for computer vision](#). In Proceedings of the May 19-22, 1975, national computer conference and exposition (pp. 589-596). ACM.

### Lecture 05 - Polygon Triangulation ([slides](#))

Date: January 28, 2019

Required Reading:

- [BCKO, 3.1-3.3](#)

Optional Reading:

- [Mount, Lecture 6 \(pg. 32-38\)](#)
- Garey, M. R., Johnson, D. S., Preparata, F. P., & Tarjan, R. E. (1978). [Triangulating a simple polygon](#). Inform. Process. Lett., 7, 175-179.
- Lee, D. T., & Preparata, F. P. (1977). [Location of a point in a planar subdivision and its applications](#). SIAM Journal on computing, 6(3), 594-606.
- A particularly famous solution: Chazelle, B. (1991). [Triangulating a simple polygon in linear time](#). Discrete & Computational Geometry, 6(3), 485-524.

[Lecture 06 - low-D Incremental LP \(slides\)](#)

Date: January 30, 2019

Required Reading:

- [BCKO, 2.4,4.2-4.3](#)

Optional Reading:

- [Mount, Lecture 7 \(pg. 39-42 -- skip the section on point-line duality for now\)](#)

[Lecture 07 - low-D Randomized LP \(slides\)](#)

Date: February 04, 2019

Required Reading:

- [BCKO, 4.3-4.4](#)

Optional Reading:

- [Mount, Lecture 8 \(pg. 45-53\)](#)
- Seidel, R. (1991). [Small-dimensional linear programming and convex hulls made easy](#). Discrete & Computational Geometry, 6(3), 423-434.

[Lecture 08 - Range Trees \(slides\)](#)

Date: February 06, 2019

Required Reading:

- [BCKO, 5.1-5.5](#)

Optional Reading:

- [Mount, Lectures 31,32 \(pg. 163-174\)](#)
- Bentley, J. L. (1975). [Multidimensional binary search trees used for associative searching](#). Communications of the ACM, 18(9), 509-517.

- Chazelle, B., & Guibas, L. J. (1986). [Fractional cascading: I. A data structuring technique](#). *Algorithmica*, 1(1-4), 133-162.
- Chazelle, B., & Guibas, L. J. (1986). [Fractional cascading: II. applications](#). *Algorithmica*, 1(1-4), 163-191.

### Lecture 09 - Trapezoidal Maps (slides)

Date: February 11, 2019

Required Reading:

- [BCKO, 6.1](#)

Optional Reading:

- [Mount, Lecture 9,10 \(pg. 53-57\)](#)
- Kirkpatrick, D. (1983). [Optimal search in planar subdivisions](#). *SIAM Journal on Computing*, 12(1), 28-35.

### Lecture 10 - Point Location (slides)

Date: February 13, 2019

Required Reading:

- [BCKO, 6.2-6.3](#)

Optional Reading:

- [Mount, Lecture 10 \(pg. 57-62\)](#)
- Snoeyink, J. S. (2017). [Point location](#). In *Handbook of Discrete and Computational Geometry, Third Edition* (pp. 1005-1028). CRC Press.
- Sarnak, N., & Tarjan, R. E. (1986). [Planar point location using persistent search trees](#). *Communications of the ACM*, 29(7), 669-679.

### Lecture 11 - Voronoi Diagrams

Date: February 18, 2019

Required Reading:

- [BCKO, 7.1-7.2,7.5](#)

Optional Reading:

- [Mount, Lecture 11 \(pg. 63-70\)](#)
- Fortune, S. (1987). [A sweepline algorithm for Voronoi diagrams](#). *Algorithmica*, 2(1-4), 153.
- Guibas, L., & Stolfi, J. (1985). [Primitives for the manipulation of general subdivisions and the computation of Voronoi Diagrams](#). *ACM transactions on graphics (TOG)*, 4(2), 74-123.

## Lecture 12 - Variations on Voronoi

Date: February 20, 2019

Required Reading:

- [BCKO, 7.3-7.4](#)

Optional Reading:

- [Mount, Lecture 30 \(pg. 160-163\)](#)
- Chew, L. Paul. (1990). [Building Voronoi diagrams for convex polygons in linear expected time](#). Technical Report PCS-TR90-147, Dept. Math. Comput. Sci., Dartmouth College, Hanover, NH.
- Aggarwal, A., Guibas, L. J., Saxe, J., & Shor, P. W. (1989). [A linear-time algorithm for computing the Voronoi diagram of a convex polygon](#). Discrete & Computational Geometry, 4(6), 591-604.

## Lecture 13 - Point-Line Duality (tentative)

Date: February 25, 2019

Required Reading:

- [BCKO, 8.1-8.4](#)

Optional Reading:

- [Mount, Lecture 7 \(particular the parts on duality on pg. 41-44\)](#)
- [Mount, Lecture 14 \(pg. 80-83\)](#)
- Edelsbrunner, H., Seidel, R., & Sharir, M. (1993). [On the zone theorem for hyperplane arrangements](#). SIAM Journal on Computing, 22(2), 418-429.
- Edelsbrunner, H., & Guibas, L. J. (1989). [Topologically sweeping an arrangement](#). Journal of Computer and system sciences, 38(1), 165-194.

## Lecture 15 - Delaunay Triangulations (tentative)

Date: March 11, 2019

Required Reading:

- [BCKO, 9.1-9.2](#)

Optional Reading:

- [Mount, Lecture 12 \(pg. 70-74\)](#)
- [Chapter 2 \(Available from Shewchuk's website\)](#) of Shewchuk, J., Dey, T. K., & Cheng, S. W. (2016). Delaunay mesh generation. Chapman and Hall/CRC.

## Lecture 16 - More Delaunay (tentative)

Date: March 13, 2019

Required Reading:

- [BCKO, 9.3-9.4](#)

Optional Reading:

- [Mount, Lecture 13 \(pg. 74-79\)](#)
- Guibas, L. J., Knuth, D. E., & Sharir, M. (1992). [Randomized incremental construction of Delaunay and Voronoi diagrams](#). *Algorithmica*, 7(1-6), 381-413.

Lecture 17 - Alpha Hulls (tentative)

Date: March 18, 2019

Required Reading:

- Edelsbrunner, H., Kirkpatrick, D., & Seidel, R. (1983). [On the shape of a set of points in the plane](#). *IEEE Transactions on information theory*, 29(4), 551-559.

Contact:

Department of Computer Science  
University of Arizona  
754 Gould-Simpson  
1040 E. 4th Street  
Tucson, AZ 85721, USA  
Phone: +1-520-621-3153

Email: [username]@email.arizona.edu, my username is josh.

Last Updated: 2019-02-11 12:58:03 -0700